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A non-linear time-series analysis approach to identify thresholds in associations between population antibiotic use and rates of resistance

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50 Abstract

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52 Balancing access to antibiotics with control of antibiotic resistance is a global public health
53 priority. Currently, antibiotic stewardship is informed by a ‘use it and lose it’ principle, in
54 which population antibiotic use is linearly related to resistance rates. However, theoretical
55 and mathematical models suggest use-resistance relationships are non-linear. One explanation
56 is that resistance genes are commonly associated with ‘fitness costs’, impairing pathogen
57 replication or transmissibility. Therefore, resistant genes and pathogens may only gain a
58 survival advantage where antibiotic selection pressures exceed critical thresholds. These
59 thresholds may provide quantitative targets for stewardship: optimising control of resistance
60 while avoiding over-restriction of antibiotics. We evaluated the generalisability of a non-
61 linear time-series analysis approach for identifying thresholds using historical prescribing and
62 microbiological data from five populations in Europe. We identified minimum thresholds in
63 temporal relationships between use of selected antibiotics and rates of carbapenem-resistant
64 *Acinetobacter baumannii* (in Hungary), extended spectrum β -lactamase producing
65 *Escherichia coli* (Spain), cefepime-resistant *Escherichia coli* (Spain), gentamicin-resistant
66 *Pseudomonas aeruginosa* (France), and methicillin-resistant *Staphylococcus aureus*
67 (Northern Ireland) in different epidemiological phases. Using routinely generated data, our
68 approach can identify context-specific quantitative targets for rationalising population
69 antibiotic use and controlling resistance. Prospective intervention studies restricting antibiotic
70 consumption are needed to validate thresholds.

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Introduction

Antimicrobials have facilitated improvements in health and food-security worldwide. However, excessive use has promoted antimicrobial resistance (AMR), undermining many aspects of healthcare and generating new disease burdens.¹⁻⁴ While decisions around antimicrobial use are made by individual prescribers and patients, consequences of over-use are only fully apparent across populations.⁵ Competing needs and non-exclusivity lead to a ‘tragedy of the commons’.^{1,2} The Global Action Plan on AMR therefore emphasises cross-societal efforts to conserve the current stock of effective antimicrobials.⁶ Antimicrobial stewardship aims to control AMR by reducing inappropriate use, while ensuring access to effective therapy.² There is growing evidence that reducing population use of antimicrobials selecting for resistance, can effectively reduce AMR.⁷ However, over-restriction may be counter-productive: use of alternative antimicrobials may increase in response, leading to new selection pressures or resistance problems.⁸ Balancing the benefits and risks of antimicrobials in healthcare requires understanding of their effects on AMR at population scales.⁹⁻¹¹

Most empirical evidence has considered linear use-resistance relationships.¹²⁻¹⁶ Although useful for identifying the most salient selection pressures in a population,¹² theoretical and mathematical models suggest non-linear relationships are more likely.^{9-11,17} In particular, selection pressures may only impact on resistance rates, where volumes of antibiotic use in the population are above minimum thresholds. Potential explanations for minimum thresholds, include: antibiotic substitution with changes in use,⁸ associations between the strength of selection pressure and induction of co-resistance,¹⁸ differential effects on sub-populations within bacterial species,¹⁹ or ecological niches,²⁰ and the ‘total use thresholds’ hypothesis.⁹ The latter concept arises from the observation that resistance genes are commonly associated with fitness costs impairing pathogen replication or transmissibility.²¹ Resistant pathogens may therefore only gain a survival advantage over susceptible organisms, where selection pressures from antibiotic use outweigh fitness costs.⁹ If identified, minimum thresholds may offer important targets for antibiotic stewardship, indicating an upper limit of safe population antibiotic use which does not increase resistance within populations.

Non-linear relationships between fluoroquinolone use and resistant *E.coli* and *Staphylococcus aureus* have been reported.^{20,22} We have shown that reducing antibiotic use to below minimum thresholds predicted shifts in the molecular and clinical epidemiology of *S. aureus* and *Clostridium difficile*.²³⁻²⁵ However, early findings suggest antibiotic use-resistance relationships are likely to depend upon the clinical population,^{9,23,25} pathogen genotypes,²⁴ intensity of infection control,²³ and transmission dynamics.¹¹ Moreover, fitness costs associated with different resistance genes are variable.²¹ If fitness costs are low, or attenuated through epistasis²⁶ or compensatory mutations,²⁷ resistance may persist despite removing previously important antibiotic selection pressures.²⁸ A generalisable method for finding minimum thresholds should therefore provide context-specific results, have relatively low-informational demands, and allow for iteration.

Here, we examined the generalisability of a non-linear time-series analysis methodology for identifying minimum threshold in use-resistance associations. Using routinely generated data from five European centres, we show this pragmatic approach can provide population-specific quantitative targets for antimicrobial stewardship for a variety of resistance outcomes, epidemiological phases, transmission dynamics, and clinical populations.

Results

Identifying non-linear temporal relationships: from experiment to application

In a Monte Carlo experiment we compared the ability of linear and non-linear time-series analysis (Multivariate Adaptive Regression Splines, MARS) to identify pre-defined relationships between simulated explanatory and outcome time-series (Supplementary Figure 1). Non-linear time-series analysis (NL-TSA) accurately identified both truly linear and non-linear associations. However, linear time-series analysis provided biased estimations and overall poorer data-fit if relationships were non-linear.

NL-TSA models applied to retrospective time-series data from five European study populations (examples 1-5), frequently identified minimum thresholds in antibiotic use-resistance relationships, (figures 1-5 and Supplementary Table 1). ‘Ceiling effects’, in which further increases in explanatory variables did not affect resistance rates, were found at high-levels of use of some antibiotics and hand hygiene. Non-linearities in autoregression and population interaction terms further indicated the complexity of transmission dynamics within and between clinical populations.

Example 1: Carbapenem-resistant *Acinetobacter baumannii* (Debreceen, Hungary)

We examined ecological determinants of carbapenem-resistant *A. baumannii* (CRAb) in a tertiary hospital population in Debreceen, Hungary (figure 1). Between Oct 2004 and Aug 2016 (n=143 months), incidence density of CRAb increased from a 12-month average of 0.14 to 9.43 cases per 10 000 OBDs, while that of carbapenem-susceptible *A. baumannii* (CSAb) remained relatively constant. There were no planned antibiotic stewardship interventions in the study period. We observed increasing use of broad-spectrum antibiotics, including a tripling in carbapenem use, and more recent escalation in colistin use.

Carbapenem resistance in this setting was conferred predominantly by *bla*_{OXA-23}-like carbapenemases, while *bla*_{OXA-24}-like genes occurred sporadically.²⁹ CRAb were significantly more likely to be resistant to ciprofloxacin, gentamicin, amikacin, piperacillin-tazobactam and ceftazidime than CSAb (Supplementary Table 2), although susceptibility testing for the latter two agents was discontinued in 2013 as recommended by EUCAST. Vector autoregression models found that colistin use followed, rather than predicted, variation in CRAb incidence density. Use of carbapenems, fluoroquinolones, piperacillin-tazobactam, third generation cephalosporins (3GC), and aminoglycosides were considered potential explanatory variables.

Previous CRAb incidence density and recent hospital use of carbapenems, piperacillin-tazobactam, and fluoroquinolones were explanatory variables in the best-fit ($R^2=0.86$) non-linear TSA model (Supplementary Table 1). In an almost identical model with poorer trade-off of data fit and model complexity (higher Modified Generalised Cross Validation statistic), fluoroquinolone use was replaced by the effect of 3GC use above a threshold of 36 (95% CI, 30 to 41) DDDs per 1000 OBDs (coefficient, 95% CI: 0.111, 0.018 to 0.203; $p=0.019$; lag 3).

In this setting increases in CRAb added to, rather than replaced, CSAb, suggesting CRAb occupied new ecological niches. Strong autoregression in the CRAb time-series was consistent with substantial within-hospital transmission.²⁹ CRAb incidence density increased when population use of carbapenems, piperacillin-tazobactam, fluoroquinolones, and 3GC exceeded minimum thresholds. By the end of the study period, use of fluoroquinolones had reduced to below threshold. However, CRAb could be further controlled by reducing use of

carbapenems, 3GC, and piperacillin-tazobactam, from present levels to respective thresholds (table 1).

Example 2: Extended spectrum β -lactamase producing *E. coli* (Orihuela, Spain)

We examined variables temporal associated with the percentage of *E. coli* producing ESBL (%Ec-ESBL+) in connected district general hospital and community populations of Orihuela, Spain, between Jul 1991 and Oct 2016 (n=304 months, figure 2). Limited outbreaks of ESBL-producing *E. coli* were noted from 1998, but from 2002 the %Ec-ESBL+ increased rapidly alongside escalating use of fluoroquinolones and co-amoxiclav. While use of these agents later stabilised or declined, hospital use of third-generation cephalosporins continued to increase.

Over the study period, *bla*_{CTX-M} genes were common in *E. coli* across Spain, with dissemination of the CTX-M-15-producing O25b-ST131 clone and clonally unrelated CTX-M-14-producing strains identified.^{30,31} Acquisition of fluoroquinolone resistance was a key step in the evolution of dominant *bla*_{CTX-M-15} containing sub-clones of O25b-ST131.³² Consistent with this, 81% of ESBL-producing *E. coli* in Orihuela were non-susceptible to ciprofloxacin. They were also significantly more likely to be resistant to co-trimoxazole, co-amoxiclav and aminoglycosides compared to non-ESBL *E. coli* (Supplemental Table 3). Vector autoregression models demonstrated bidirectional interactions between community and hospital %Ec-ESBL+ and that use of piperacillin-tazobactam and carbapenems followed, rather than predicted, changes in %Ec-ESBL+. In separate hospital and community models, %Ec-ESBL in the other population was considered as an explanatory variable.

In the best-fit model ($R^2=0.62$) hospital %Ec-ESBL+ was predicted by prior %EcESBL in hospital and community, and hospital use of 3GC, and fluoroquinolones exceeding minimum thresholds (Supplementary Table 1). A potential ‘ceiling’ effect was noted at high-levels of fluoroquinolone use, meaning that when use exceeded a second upper threshold, further increases in %Ec-ESBL+ were small. An initial decrease in %Ec-ESBL+ where fluoroquinolone use was between 151 and 161 DDDs per 1000 OBDs reflected uncertainty around this ceiling threshold, which may be resolvable with additional data. In the model for community %Ec-ESBL+ (R^2 0.767), associations were identified with hospital %Ec-ESBL+, and community use of fluoroquinolones and co-amoxiclav above minimum thresholds.

Autoregressive and population interaction effects suggested the importance of horizontal transmission of ESBLs, with predominant influence of community on hospital epidemiology. Population use of broad-spectrum beta-lactams and fluoroquinolones were important explanatory variables in both settings. In the community, use of fluoroquinolones had fallen below threshold levels and %Ec-ESBL+ had started to decrease by the end of the study. However, translating thresholds into antibiotic stewardship targets (table 1) suggested further restricting community co-amoxiclav use by 31% and hospital use of fluoroquinolones (-41%) and 3GC (-21%).

From best-fit models, we created 24-month projections for %Ec-ESBL+ in the hospital and community under different antibiotic stewardship options, and compared these to expected %Ec-ESBL+ under a ‘business as usual’ scenario of antibiotic use (Supplementary Figure 2). Immediate restriction of hospital use of fluoroquinolones and 3GCs to thresholds was predicted to cause an abrupt and sustained reduction in hospital %Ec-ESBL+ from 9.89% to 2.35% ($p<0.0001$) and, due to population interactions, a gradual reduction in community %Ec-ESBL+ from 7.11% to 3.69% ($p<0.0001$). Limiting community co-amoxiclav use to

threshold levels was predicted to cause a small reduction in community %Ec-ESBL+ but not to affect hospital epidemiology.

Example 3: Cefepime-resistant *Escherichia coli* (Seville, Spain)

We examined ecological variables explaining cefepime resistance among urinary or invasive *E.coli* infections (%Ec-FepR) in a tertiary hospital in Seville, Spain. Between March 2008 and December 2016 (n=108 months) %Ec-FepR fell from 12.6% to 7.9% (figure 3). Cefepime use was low, declining from 4.4 to 1.6 DDDs per 1000 OBDs with thrice-weekly (Jan 2012, audit1) and daily (Jan 2014, audit2) prescription audits. By contrast, previously declining use of 3GC increased from January 2013 when they replaced co-amoxiclav and ciprofloxacin as first-line empirical therapy for intra-abdominal or urinary infections.

Resistance to cefepime in *E. coli* is mostly conferred by ESBLs with high affinity for cefepime (TEM-, SHV- and CTX-M-types). In addition to those agents hypothesised to predict ESBL-producing *E. coli* (see example 2), we considered the role of piperacillin-tazobactam.¹³ Due to low rates of cefepime prescribing, we grouped this with 3GC use. We introduced variables for antibiotic auditing interventions and for revised susceptibility breakpoints (Oct 2014).³³

The final non-linear model (R^2 0.30) identified associations with %Ec-FepR 12 months prior (seasonal effect) and use of third- or fourth-generation cephalosporins and fluoroquinolones above minimum thresholds (Supplementary Table 1). A significant interaction term between %Ec-FepR in the previous month (autoregression, lag 1) and the second antibiotic auditing intervention suggested a gradual effect of the audit in reducing %Ec-FepR.

Reductions in third- and fourth-generation cephalosporins and fluoroquinolone use to below minimum thresholds explained modest declines in %Ec-FepR between 2008 and 2012. Partial reversal in this trend was consistent with increasing use of 3GC towards the end of the study period. %Ec-FepR could be controlled further by reducing third- and fourth-generation cephalosporin use by 41% (table 1).

Example 4: Gentamicin-resistant *Pseudomonas aeruginosa* (Besançon, France)

We examined ecological variables explaining rates of gentamicin-resistant *P. aeruginosa* (GRPa) among adult and paediatric admissions to a tertiary hospital in Besançon, France (figure 4). Between Jan 1999 and Dec 2014 (n=192 months), incidence density of GRPa decreased from 14.0 to 3.4 cases per 1000 OBDs, and the proportion of *P. aeruginosa* isolates resistant to gentamicin declined from 63% to 16%.

Aminoglycoside modifying enzymes (AMEs) are the most common mediators of aminoglycoside resistance in *P. aeruginosa*; with acetyltransferases (e.g. *aac(6')-Ib*) and nucleotidyltransferases (e.g. *ant(2'')-Ia*) most frequent in Europe.³⁴ Since related genes in mobile genetic elements encode AMEs and β -lactamases, β -lactam use may also predict aminoglycoside resistance.³⁵ In previous analyses from Besançon, aminoglycosides, cefepime and fluoroquinolones were predictors of MexXY-OprM overproduction in *P. aeruginosa*.³⁶ GRPa isolates were also more likely to overproduce the chromosomally-encoded AmpC cephalosporinase (56% vs. 20%; $p<0.001$) and be multi-drug resistant (65% vs. 13%; $p<0.001$). We hypothesized that GRPa incidence density may be predicted by use of aminoglycosides, fluoroquinolones, extended-spectrum penicillins with β -lactamase inhibitors, carbapenems, monobactams, and third- and fourth-generation cephalosporins.

Given potential intra-class differences in promoting resistance, we grouped use of gentamicin and tobramycin separately from that of amikacin.

In the best-fit model ($R^2=0.86$), GRPa incidence density was strongly predicted by incidence density in the previous month, and hospital use of gentamicin/tobramycin and fluoroquinolones above minimum thresholds (Supplementary Table 1). No independent association with Amikacin use was identified.

Declining GRPa was largely explained by falling inpatient use of gentamicin/tobramycin, and, to a lesser extent, fluoroquinolones. Use of both drug groups was maintained below minimum thresholds from around 2007. Continuing decreases in GRPa incidence density were at least partially explained by autocorrelation at lower incidence densities. Reciprocal increases in gentamicin-susceptible *P. aeruginosa* over the same period, and moderate inverse correlation ($r=-0.55$), suggest competition for the same niche as GRPa. Gentamicin/tobramycin and fluoroquinolone use should be maintained below thresholds to control GRPa.

Example 5: Methicillin-resistant *Staphylococcus aureus* (Antrim, Northern Ireland)

We evaluated ecological variables explaining incidence density of MRSA clinical isolates in adult admissions to a district general hospital in Antrim (Jan 2005 to Sep 2013, $n=105$ months). Between 2005 and mid-2008, incidence density of MRSA clinical isolates remained stable at c.3.0 per 1000 OBDs (figure 5). Following restrictiong fluoroquinolones (January 2008) and intensification of hand-hygiene, burdens fell to 1.64 cases per 1000 OBDs by 2013.

The epidemic hospital MRSA clonal complex CC22, predominated in Northern Ireland during the study period: its success attributed to an ability to acquire mobile genetic elements carrying multiple resistance genes, with limited fitness costs.³⁷ Following prior linear time-series analyses from the region,¹⁴ we hypothesised use of fluoroquinolones, 3GC, co-amoxiclav, and macrolides could be important predictors of MRSA epidemiology.

In the best-fit model ($R^2=0.53$), MRSA incidence density was positively associated with rates of MRSA in the previous month and use of fluoroquinolones, 3GC, and co-amoxiclav exceeding minimum thresholds (Supplementary Table 1). An inverse relationship was seen with increased hospital use of alcohol-based hand rub (ABHR) up to 6.9 Litres per 1000 OBDs, above which further increases in ABHR use was not associated with further declines in MRSA.

Declining MRSA incidence density was partly explained by deliberate restriction of fluoroquinolone use, and concurrent declines in co-amoxiclav and 3GC. Strong autoregression, and inverse association with ABHR use, were consistent with importance of infection control measures in interrupting horizontal transmission. Reversal of previous declines in fluoroquinolone use were seen by the last year of study. Findings suggested maintaining use of co-amoxiclav and 3GC under thresholds, use of ABHR at threshold levels, and further restriction of fluoroquinolones (table 1).

Discussion

Using a non-linear time-series analysis (NL-TSA) approach, we found empirical evidence of non-linear relationships between population antibiotic use and resistance rates in five European settings. The method was generalisable to different clinical populations, resistant pathogens, definitions of resistance burdens, and epidemiological phases. We demonstrated that identification of minimum thresholds, and associated confidence intervals, could provide population-specific quantitative targets for antibiotic stewardship.

Our approach builds upon earlier work using linear time-series analysis to explain temporal relationships between antibiotic use and resistance.¹²⁻¹⁶ NL-TSA shares a number of strengths, including: low-informational demands; ease of reiteration as new data becomes available; adjustment for the non-independence of serial observations and stochasticity inherent to time-series of communicable diseases; identification of temporality in associations and ‘lagged’ effects; and integration of impacts of multiple exposures.¹² Additionally, NL-TSA reveals non-linear relationships, providing more accurate understanding of how modifying antibiotic use, infection control or other exposures is likely to affect resistance. Limitations of NL-TSA include: the need for longer time-series than linear TSA; the potential for spurious thresholds in areas of limited data or extremes of the exposure variable range; and difficulty in identifying thresholds in situations of stable resistance and prescribing. We note the poorer predictive performance of some models (e.g. example 3), may be explained by absence of data on infection prevention and control activities, and resistance levels in interacting populations.

Our findings may have important implications for antibiotic stewardship. In general, impacts of changes in antibiotic use on resistance vary dependent upon the antibiotic use level. More specifically, minimum thresholds may be interpreted as an upper limit for ‘safe’ population antibiotic use which does not appear to substantially increase resistance rates at the population level. Alternative theories may suggest the threshold indicates: a maximum level of selection pressure not conferring a survival advantage to resistant pathogens to spread within populations or ecological niches,^{8,12} or strong enough to induce resistance;¹⁸ or a minimum level of use, below which antibiotic substitution creates equivalent or greater selection pressure.⁸ Crucially, they may provide quantitative targets for balancing the need to access therapies with control of resistance, analogous to ‘quotas’ applied to other natural resources which seek to maximize extracted value while maintain a non-declining stock.^{1,2,38} Moving from qualitative targets of reducing use, to quantitative targets may also aid operational effectiveness. Targets appear to work best if pragmatic, collaborative and iterative.³⁹ Complete restriction of use of agents is rarely feasible: in balancing access to effective therapies with control of resistance, quantitative targets could align interests of clinicians and antimicrobial management team.⁴⁰

We emphasise the need for caution with interpretations of thresholds. Firstly, thresholds should offer guidance rather than strict limits. Uncertainty around thresholds is variable, as reflected in width of associated confidence intervals. Narrower confidence intervals around threshold locate with reasonable precision the level of antibiotic use at which effects on resistance are substantially altered. Wider intervals may indicate insufficient data, or the influence of additional explanatory variables. In rare instances of multiple closely occurring thresholds in a single functional relationship, the width of confidence intervals may be underestimated and should be interpreted with particular caution. We suggest a pragmatic approach, of interpreting thresholds depending upon the policy scenario. Where the priority is strict control of resistance a conservative approach of limiting use to the lower limit of the

threshold confidence interval is advisable. Where excessive restriction is a concern, the standard approach of limiting use to the point estimate of the threshold is likely to offer the best balance between restriction and control of resistance. Secondly, changes in molecular epidemiology under sustained antibiotic selection pressures, such as compensatory mutations minimising fitness costs,^{26,27} or strain replacement,^{24,25} may mean thresholds vary by epidemiological phase and time. Variation in thresholds across populations can be anticipated, reflecting host, environment, and organism factors.²³⁻²⁵ Therefore, models based on local data and iterative analysis is necessary to ensure time and context-specific guidance. Thirdly, it is important not to assume that all antibiotic use below thresholds is safe, since antibiotic exposures may be important for individual patients, or cause unseen change in reservoirs of resistant pathogens in environment or hosts.

Potential foci for further research include: evaluating the consistency of thresholds for specific antibiotic use-resistance combinations across different settings and identifying factors affecting thresholds; applying NL-TSA to composite indices of resistance;^{41,42} use of Bayesian approaches in selection of explanatory variables and analysis with short time-series or rare resistance outcomes;⁴³ and prospective studies to validate the effectiveness of quantitative targets in antibiotic stewardship.

We have illustrated how non-parametric time-series models based on empirical data can identify non-linear relationships between population antibiotic use and resistance burdens. Further we have shown how identification of population-specific minimum thresholds may guide rational compromises between control of resistance and access to therapeutics. With the increasing availability of electronic surveillance and healthcare systems, this approach offers a useful tool for sustaining the effectiveness of current antimicrobials in many areas of the world.

Methods

Design and study populations

This was a multi-centre time-series study. We used multivariable non-linear time-series analysis to quantify associations between ecological exposures, including population use of antibiotic groups, and rates of antibiotic-resistant infections in five populations from France, Hungary, Northern Ireland (UK), and Spain (Supplementary Table 5).

The populations and resistance outcomes were a purposive sample, chosen to reflect varying epidemiological scenarios, clinical settings, and resistant infections in European centres participating in the THRESHOLDS (THReshold ESTimation to Help Optimise Local Decisions on antibiotic Stewardship) study group. This collaborative aims to further the development of time-series analysis for understanding antibiotic resistance and planning antibiotic stewardship. Members included centres with prior experience in applying linear time-series approaches. Investigators were asked to identify an important resistance problem in a defined clinical population from their region. Minimum data requirements were consistent microbiological and prescribing data across a minimum of 60 monthly observations (5 years). Duration of time-series was defined by the longest period of consistent data for a minimum data set of the outcome and candidate explanatory variables.

For each population we described the regional scenario for the chosen outcomes, the theoretical basis for inclusion of candidate explanatory variables, findings from the non-linear time-series analysis, and how these could inform local antibiotic stewardship policy.

Outcome and explanatory time series

The outcome time-series for each population were: carbapenem-resistant *Acinetobacter baumannii* (Debrecen, Hungary); extended spectrum β -lactamase producing *Escherichia coli* in hospital and community (Orihuela, Spain); cefepime-resistant *Escherichia coli* (Seville, Spain); gentamicin-resistant *Pseudomonas aeruginosa* (Besançon, France); and methicillin-resistant *Staphylococcus aureus* – MRSA (Antrim, Northern Ireland). Cases were defined microbiologically as isolates from all relevant body sites not identified as infection control specimens and meeting consistent criteria for resistance or resistance mechanism (see supplemental file for details). Isolates from the same patient identified within 30 days of a prior isolate with the same organism were considered part of the same infectious episode and de-duplicated. Outcomes were expressed, where possible, as monthly incidence density of resistant infections (cases per 1000 or 10,000 occupied bed days, OBDs). Where there were large changes in testing frequency or organism identification over time, we defined resistance as a percentage of clinical isolates from the same organism with any susceptibility pattern.

The primary explanatory variables were monthly population use of antibiotic agents classified by pharmacological sub-group of antibacterials for systemic use (J01) in the 2016 WHO/ATC index, and expressed as defined daily doses (DDDs) per 1000 OBDs (hospital) or 1000 inhabitant-days (community). Candidate antibiotic sub-groups were identified *a priori*, on the basis of regional co-resistance profiles, molecular epidemiology in the region, reviews and prior evidence on individual or population level risk factors for acquisition of the resistant infection. We included separate time-series for individual antibiotic agents or chemical sub-groups only where there were strong theoretical grounds for investigating independent associations, such as prior evidence of variable within-class actions or targeting within antibiotic stewardship interventions.

In addition, we incorporated autoregressive terms capturing association between current incidence density and incidence density in recent months. Where available, we incorporated infection prevention and control (IPC) variables such as use of alcohol-based hand-rub. Dummy variables were added to capture immediate and gradual impacts of changes in laboratory methods or other planned interventions. We considered lags in association of up to 6 months and seasonal autoregressive terms (lag 12).

Data collection and laboratory procedures

In all centres, microbiological and prescribing and IPC data were extracted from electronic databases maintained for routine healthcare activities. Data were anonymised and aggregated before electronic submission to the THRESHOLDS study group. Meta-data on population characteristics, IPC activities, antibiotic stewardship interventions and resources for control of antibiotic resistance were captured using a standardised questionnaire.

Pathogens were identified using standard laboratory methods. Susceptibility testing was by disc-diffusion (Besançon, Debrecen, Antrim) or broth microdilution (Seville, Orihuela). Isolates were defined as resistant if not susceptible to an antibiotic agent according to zone diameter (for disc-diffusion) or minimum inhibitory concentration (MIC, for broth microdilution) breakpoints as recommended by the European Committee on Antimicrobial Susceptibility Testing (EUCAST) or Clinical & Laboratory Standards Institute (CLSI). Details of standards used, and deviations from EUCAST or CLSI criteria are detailed in table i. Known changes in breakpoints and laboratory methods were adjusted for in time-series analysis.

Statistical methods

In the following sections we provide a technical exposition of the statistical methods used. We offer here, a brief description for the general reader.

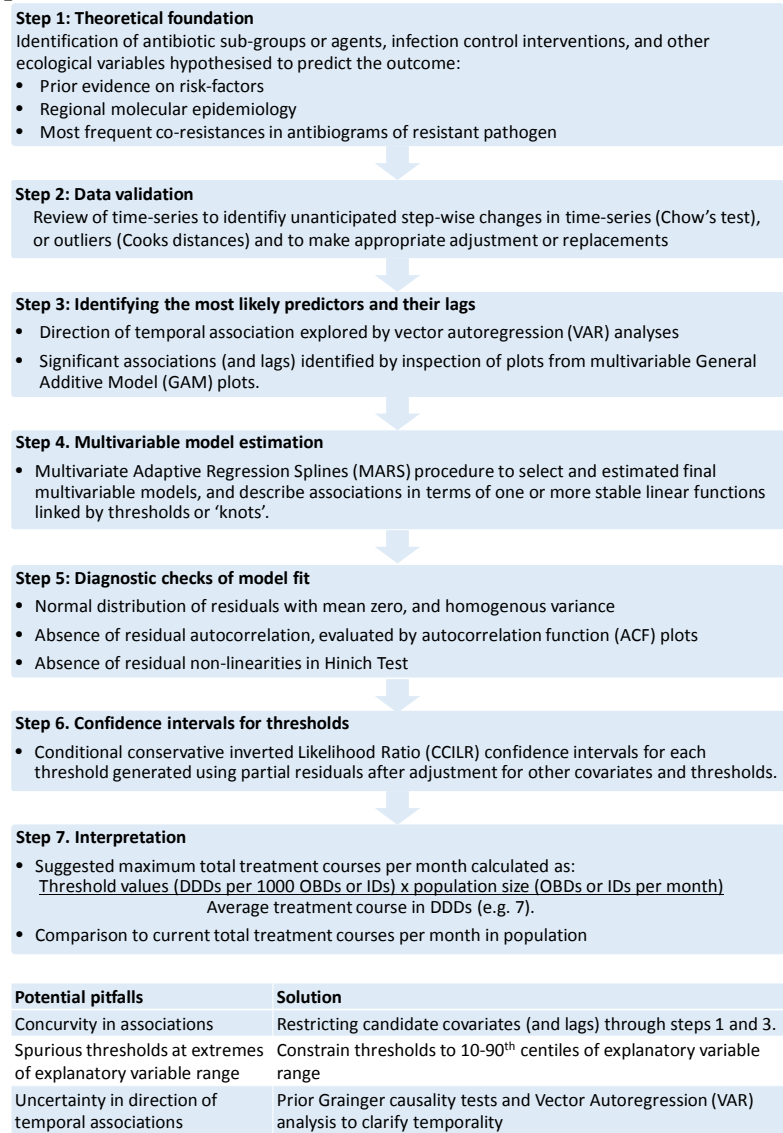
Before applying non-linear time-series analysis (NL-TSA) to real-world datasets from study populations, we performed a statistical, Monte-Carlo, experiment to illustrate its advantages over, more familiar, linear TSA. We applied both linear and non-linear TSA to computer-simulated time-series, where the relationship between the outcome and explanatory time-series was known. Three types of relationship were explored: a linear relationship; a non-linear relationship without correlations between successive data points in time-series (autoregression), and a non-linear relationship with autoregression; By running this experiment over 10,000 simulated datasets for each type of relationship we evaluated the typical ability of linear and non-linear TSA to describe the relationships accurately.

We next applied a seven-step non-linear time-series analysis approach to resistance problems in study populations (figure 6).

Mirroring more familiar regression techniques, we started by defining a set of explanatory variables including antibiotic use, infection control, population interactions, alongside terms for autoregression. This set was defined by (a) expert opinion informed by prior risk-factor studies, molecular epidemiology in the region; and (b) inspection of resistance profiles of the pathogen of interest. We consider delays between changes in explanatory time-series and associated change in outcome time-series (lags) of up to 6 months. Before analysis we checked time-series and make adjustments for extreme values (outliers) or unexpected shifts in mean (structural changes). We also used vector autoregression (VAR) models to help distinguish any reverse causality in relationships between explanatory and outcome series:

this might occur, for example, if prescribing behaviour was altered by resistance rates in the population in previous months. Next we restrict the set of explanatory variables, and lags, to be put into final multivariable models. We use a procedure that fits smooth functions to relationships between explanatory and outcome time-series, and allows visual inspection of likely significant associations. After identifying the most promising explanatory variables (and lags) we enter these into a Multivariate Adaptive Regression Splines (MARS) model which both identifies significant predictors, and defines any non-linear relations as a series of linear relationships connected by ‘knots’ or thresholds. Model fit for MARS is checked by ensuring residuals were normally distributed without unexplained non-linearities. Confidence intervals around each threshold were fit by a conditional conservative inverted likelihood ratio (CCILR) method, using partial residuals. Finally, we converted thresholds from models into suggested maximum total treatment courses per month in the population by multiplying model thresholds by the size of the population and dividing by an average treatment course.

Figure 6: Summary of the 7-step non-linear time-series methodology and potential pitfalls



To provide an example of how model findings can inform policy, for the Orihuela population, we predicted the effects of restricting antibiotic use to threshold levels compared to a ‘business as usual’ scenario of prescribing based on the last months of study. We quantify impacts of immediate restriction sustained over two years.

A technical explanation follows:

a) Comparing linear and non-linear time-series model performance

We used a Monte-Carlo experiment to compare the ability of linear (Ordinary Least Squares, OLS) and non-linear (Multivariate Adaptive Regression Splines, MARS) time-series models in identifying various pre-defined functional relationships between simulated explanatory and outcome time-series. We hypothesised that for time-series related by simple linear processes MARS and OLS regression methods would perform equally well, but that only MARS would accurately identify non-linear associations. We generated 10,000 simulated datasets using simple stochastic processes incorporating the following pre-defined functional relationships:

(i) Non-autoregressive without threshold

$$y_t = -4 + 2x_t + u_t \quad u_t \sim N(0, \sigma^2 = 0.02) \quad \forall t = 1, \dots, 200$$

(ii) Non-autoregressive with threshold

$$\begin{cases} \text{if } x_t \leq 2: & y_t = u_t & u_t \sim N(0, \sigma^2 = 0.5) \\ \text{if } x_t > 2: & y_t = -4 + 2x_t + u_t & u_t \sim N(0, \sigma^2 = 0.5) \end{cases} \quad \forall t = 1, \dots, 200$$

(iii) Autoregressive with threshold

$$\begin{cases} \text{if } x_t \leq 0: & y_t = 0 + \rho y_{t-1} + u_t & u_t \sim N(0, \sigma^2 = 0.05) \\ \text{if } x_t > 0: & y_t = 0 + \rho y_{t-1} + 1x_t + u_t & u_t \sim N(0, \sigma^2 = 0.05) \end{cases} \quad \forall t = 1, \dots, 200$$

Where:

x_t is the explanatory (independent) time-series variable at time t
 y_t is the outcome (dependent) time-series variable at time t
 u_t is the error term at time t , with Normal distribution, zero mean and variance σ^2
 ρy_{t-1} is an autoregressive term or order 1 (i.e. dated at $t-1$) with $\rho = 0.25$

For each dataset we fitted both linear and non-linear time-series analyses, and recorded sample parameter estimates (a constant, b slope, and s^2 as the estimate of population variance) and a measure of goodness of fit (R^2). Histograms were created illustrating the distributions of R^2 values and parameter estimates from both linear and non-linear models. Visual comparison was made to pre-defined parameter values to identify bias in parameter estimates. We used a t-test of mean difference for independent samples to compare model performance based on R^2 values.

b) Applications of non-linear time-series analysis to real-world datasets

We applied a seven-step approach to generate non-linear time-series models describing how contemporaneous and prior population antibiotic use, and other ecological variables, explain monthly variation in clinical burdens from antibiotic-resistant infections in five European centres.

610
611
612
613 *Step 1: Theoretical foundation*

614 Participating centres identified *a priori* a minimum dataset of antibiotic sub-groups or agents
615 they considered most likely to affect the epidemiology of the resistant organism under
616 investigation (target organism). Decisions were based upon: previous empirical evidence of
617 risk factors and molecular epidemiology in the study region or related contexts. Additionally,
618 using antibiogram data from the study period and population, we reviewed co-resistances to
619 other antibiotics among isolates of the target organism with and without the resistance under
620 investigation. We considered antibiotics with the largest absolute rates of co-resistance in the
621 resistant isolates to be most likely to exert significant selection pressures.^{44,45} Consensus on
622 the list of potential predictive variables was found through discussion among all
623 THRESHOLDS study group members.

624 Where data was available we integrated additional explanatory variables on hospital activity
625 or infection control activities, associated with the outcome variable in previous studies.

626
627 *Step 2: Data validation*

628 To ensure consistent time-series we first accounted for known changes in exogenous
629 conditions, such as changes in laboratory method. We captured immediate and gradual effects
630 by entering a dummy variable (0 in months before the change, 1 in months after change) and
631 its interaction with an autoregressive term, as explanatory variables. We then reviewed time-
632 series to detect possible unknown measurement errors as follows. Visual inspection identified
633 potential structural changes (seen as large step-wise change in mean for instance) or outliers
634 (seen as values deviating substantially from surrounding values). Successive Chow tests were
635 applied to automatically detect the most probable dates of structural changes in the time-
636 series and, where necessary, to disaggregate the sample into two or more segments, each with
637 a stable mean. For each segment we applied an outlier detection technique using the
638 following criterion: an observation was considered as an outlier if Cook's distance at this
639 point was greater than five times the mean of Cook's distances of all the observations of the
640 segment. Finally, we replaced outlier values with the mean of the three preceding and three
641 following observations.

642
643 *Step 3 Identifying the most likely predictors and their lags*

644 Given the potentially complex relationships between ecological variables under investigation
645 we sought to refine our understanding of potential associations before applying final
646 multivariable non-linear models.

647
648 Firstly, situations of reverse causality could exist when ecological exposures - such as rates of
649 infections with resistant pathogens connected populations, or use of some antibiotic groups in
650 a given population - respond to, rather than predict, rates of resistance. In order to minimise
651 this risk, we tested direction of temporal relationships between explanatory and outcome
652 time-series by applying Granger-causality analysis and Vector Autoregression (VAR)
653 models. Secondly, non-linear models of the type used in this study are potentially complex
654 and difficult to extract form the data if too many predictors are used at the same time.
655 Therefore, we carried out an additional *a priori* data-based selection of candidate explanatory
656 variables and lags (the lag refers to the delay in months between change in exposure and
657 associated change in outcome). This was done through inspection of outputs from fitting a
658 General Additive Model (GAM) to the data. GAM is a very general procedure that can be

used for the identification of the most likely predictors, since it runs a non-parametric estimation of the functional relationships between explanatory (x) and outcome (y) time-series, based upon iterative data fitting, rather than prior assumptions. It also allows for variability in the functional relationships across different values of the explanatory variables and can therefore capture non-linear associations between ecological variables and resistance outcomes.⁴⁹ In particular, we used the GAM procedure in the SCAB34S Splines module (available in SCA Workbench, Scientific Computing Associates Corp, Illinois, USA) to define the relationship between p explanatory (x) and the outcome (y) time-series as a sum of smooth, or spline, functions:

$$E(y|x_1, x_2, \dots, x_p) = s_0 + \sum_{j=1}^p s_j(x_j)$$

where ($s_j(x_j)$) are the spline functions; they were standardised such that, after removal of free constants (s_0) their expected contribution to the outcome (y) is zero (i.e. $Es_j(x_j)=0$ for each j).

The splines were derived by a process of splitting the time-series into sections, joined at knot points, and fitting simple curves described by cubic functions to the data in each section. The GAM methodology identified the optimal combination of spline functions $s_j(x_j)$, following the iterative procedure suggested by Hastie and Tibshirani(1986).⁴⁶ Combining a local scoring algorithm and a backfitting procedure, this method converges on a solution balancing data fit with smoothness.

To identify the most relevant explanatory time-series, for each centre we started with a multivariable GAM model including all theoretically relevant variables at lags of 1 to 6 months and autoregressive terms at lags 1 and 2. We limited lags to 6-months based on widespread evidence of declining relevance of antibiotic exposures by time-since exposure, and prior experience that considerations of longer lags lead to problems of concurvity. On the basis of the GAM outputs, an explanatory variable with a specific lag was retained in the model only if its contribution was significant at a 5% level of probability (identified on contribution charts by the zero line of non-association falling outside of 95% confidence intervals around the estimate). The process was run iteratively by removing first those variables and lag combinations whose contributions were non-significant before re-running the GAM model on a reduced subset of variables and lags. The process stopped when the model contained only significant contributions of variables and lags. These constituted the restricted set of explanatory variables for entry into MARS analysis.

A further objective of applying the GAM procedure was to determine whether consideration of non-linear associations is justified in terms of improvement in predictive performance. For each explanatory variable (and lag), GAM provides a comparison of the data fit of a non-linear spline function (nl) with an analysis in which this relationship is restricted to a linear function (l). Significant improvement in goodness of fit over a linear fit is defined by an F -test, as follows:

$$F_0 = \frac{(SSR_l - SSR_{nl}) / (p_{nl} - p_l)}{SSR_{nl} / (n - p_{nl})} \sim F_{(df_{nl} - df_l), (n - p_{nl})}$$

where; SSR = Sum of squares of residuals, n = number of observations, p = number of parameters, l = linear function, and nl = non-linear spline function.

The null hypothesis that estimates from an enhanced (non-linear) model do not provide a significantly better fit than those from a linear model can be rejected where F exceeds a critical value ($\alpha=0.05$) from an F-distribution with $(p_{nl}-p_l, n-p_{nl})$ degrees of freedom.

Step 4. Multivariable model estimation

After identifying the most likely explanatory variables (and lags), and whether associations with the outcome series were linear or non-linear, we used the MARS procedure (in the SCAB34S Splines module) to obtain an easily interpretable characterization of these associations.⁴⁷ MARS is a non-parametric regression approach suitable for situations of non-linear associations that can provide more interpretable and interesting empirical results than GAM. Given our research aims, its particular advantages were: (i) the ability to identify distinct threshold values ('knots') of the explanatory variables delimiting regions (ranges of values) of individual or interacting explanatory variables within which associations with the outcome differs substantially from those in other regions; and (ii) a systematic approach for model identification and estimation, which automatically selects the combination of explanatory variables and threshold values which most efficiently explain variation in outcomes. MARS is related to, but more general than, regression tree algorithms, and has several important, interrelated advantages: (a) when thresholds may affect several explanatory variables, the final MARS model is far more synthetic, and therefore more interpretable, in terms of quantifying how each explanatory variable (e.g. antibiotic use) affects the response variable (e.g. resistance) and interacts with other explanatory variables; (b) the MARS algorithm in general deals much better with numerical data and continuous data; (c) it allows for dynamic relationships and thresholds in the dynamic dependences - especially important when analysing effects with time series data; and (d) MARS does better in extrapolating the results outside the sample data ranges of explanatory and outcome variables. These advantages are important when considering policy implications of findings for control of AMR.

MARS approximates the functional relationship between an outcome time-series (y_t) and a vector of p explanatory variables $x_t = (x_t^1 \dots x_t^p)$ as:

$$y_t = \beta_0 + \sum_{m=1}^M \beta_m b_m(x_t) + \varepsilon_t$$

where;

β_0 is a constant

β_m is the coefficient for the m^{th} basis function, $m=1, \dots, M$

$b_m(x_t)$ is the m^{th} basis function, $m=1, \dots, M$

ε_t is an independently distributed error term.

The basis functions are products of up to two truncated linear or hinge functions, describing the relationship between one or more explanatory variables and the outcome in terms of segments of stable association separated by knots or thresholds values. These interacting hinge functions allow us to identify possible interactions between variables as in Figure 1C(ii). Namely, the m^{th} basis function takes one of the following two forms:

No interaction: $b_m(x_t) = h(x_t^k, t_{k,m})$ for some $k = 1, \dots, p$

With interaction: $b_m(x_t) = h_m(x_t^k, t_{k,m}) \cdot h_m(x_t^j, t_{j,m})$ for some $k, j = 1, \dots, p, k \neq j$

where $t_{k,m}$ is the threshold value of x_t^k in the m^{th} basis function and where $h(x_t^k, t_{k,m})$ is a hinge function that takes the following form depending on whether the basis function takes effect above or below the threshold $t_{k,m}$

750 a) above the threshold: $h_m(x_t^k, t_{k,m}) = \max(x_t^k - t_{k,m}, 0)$

751 b) below the threshold: $h_m(x_t^k, t_{k,m}) = \max(t_{k,m} - x_t^k, 0)$

752

753 If no knot (threshold) is detected, then a simple linear (and therefore constant) association
754 between explanatory and outcome variable can be specified as a single function applied
755 across the total range of values of the explanatory variable.

756

757 All potentially significant explanatory variables, and associated lags, identified in previous
758 steps, were incorporated into models. Model identification and estimation proceed by an
759 automated, iterative, process:

760

761 *Forward pass:* starting with the simplest model containing only a constant basis function,
762 MARS generates a matrix of basis functions in a forward stepwise manner. Candidate base
763 functions are added in order of ability to improve model fit, until the model reaches a
764 predefined limit of complexity. The candidate basis functions are identified by a nested
765 exhaustive search looping over the existing set of basis functions, and all other possible
766 explanatory variables (or interactions) and knot positions.

767

768 *Backwards (pruning) pass:* During the subsequent pruning pass MARS removes basis
769 functions contributing least to model fit, until no significant improvement is seen in a
770 modified form of the generalized cross validation (MGCV) criterion:

771
$$\text{MGCV} = \frac{\frac{1}{N} \sum_{i=0}^n (y - f(x))^2}{1 - ((C(M) + dM)/n)^2}$$

772

773 Where; N is the number of observations,

774 $\sum_{i=0}^n (y - f(x))^2$ is the sum of square of residuals (observed - estimated y).

775 $C(M)$ is the number of parameters being fitted, M the number of non-constant basis
776 functions and $d=3$ (conventional value).

777

778 The MGCV incorporates a complexity penalty accounting for the inherent improvement in
779 explained variance associated with increasing numbers of basis-functions, and its calculation
780 allows estimates of the relative importance of each basis function. Model selection therefore
781 converges on a set of basis functions that most efficiently explain variation in antibiotic
782 resistance before a final model fit by OLS estimation.

783

784 From the output of each MARS model we generated contribution charts illustrating the
785 change in the outcome time-series across the observed ranges of explanatory variables.

786

787 *Step 5. Diagnostic checks*

788 Adequacy of model fit was defined by three criteria: (i) *Normally distributed residuals* – with
789 homogenous variance and mean equal to zero, as evaluated by a Normality test; (ii) *absence*
790 *of significant residual autoregression* – identified in lags 0 to 6 on an autocorrelation function
791 (ACF) plot; and (iii) *absence of residual non-linearities* – as evaluated by a Hinich test. In
792 addition to the MGCV we reported more familiar measures of model performance such as R^2
793 and the mean absolute percentage error (MAPE).

794

795 *Step 6: Confidence intervals (CIs) for thresholds values*

In the absence of an existing method for deriving measures of uncertainty around thresholds derived from non-parametric MARS models, we develop a procedure inspired by Hansen (2000).⁴⁸ His procedure considers a simple threshold model with only one variable affected by a threshold effect, and obtains a distribution theory for the threshold parameter (τ) from which asymptotic confidence intervals can be built. He first derives the limiting distribution of a Likelihood Ratio test (LR) for the null hypothesis that the threshold parameter $\tau = \tau_0$. He then builds confidence intervals through the inversion of LR: the $(1-\alpha)$ Inverted Likelihood Ratio (ILR) confidence interval consisting of all the possible values of τ for which the null hypothesis would not be rejected at the α level. Donayre et al. (2018) examine improvements of Hansen's ILR confidence interval, increasing its quality in finite samples with large threshold effects (i.e. when the change in slope from one side of the threshold to the other is large).⁴⁹ They show that a 'conservative modification' enlarging Hansen's ILR confidence interval is optimal. In this "conservative ILR confidence interval" the lower end of the interval is enlarged from the first value lower than τ_l for which the null hypothesis is rejected, up to τ_l ; at the upper end, it is enlarged from τ_u up to the first value greater than τ_u for which the null hypothesis is rejected. This modification provides intervals at a confidence level at least as high as the nominal one that are still informative.

We adapted this procedure for MARS estimations with more than one explanatory variable containing thresholds, and one or more thresholds per variable, by using the partial residuals –i.e. the variation in the outcome not explained by other explanatory variables and their thresholds. This allowed us to identify conservative ILR confidence intervals for each explanatory variable, conditional on all the estimated coefficients and thresholds other than the one for which the confidence interval is computed. Since in MARS all thresholds and slope coefficients are anyway selected and estimated to optimise overall model fit using conditional inference, identifying these 'conditional conservative ILR (CCILR) confidence intervals' does not impose costs to reliability. Computing confidence intervals conditional only on other thresholds, but with re-estimation of coefficients describing piece-wise associations (slopes), offers a valid alternative. In Monte Carlo simulations (results available on request) we found both approaches resulted in adequate coverage (>95% of intervals including the actual value of the threshold) but CIs were wider with a procedure with slope re-estimation and less informative for a given coverage rate. Our simulations show that the superiority of the partial residual approach is independent of the degree of correlation between antibiotic segments (values of antibiotic use over which association with the outcome is constant) where correlation is between 0% and 75%. There is some risk of very slight under coverage with the partial residual approach where correlations are $\geq 85\%$, but such high levels of correlation are unlikely unless several the functional relationship involves multiple, closely occurring, thresholds. In such situations, re-estimation of slope co-efficients is anyway not feasible. As a result, we recommend the partial residual approach, with a caution that the CI could be somewhat wider in specific and infrequent situations where multiple close thresholds for the same independent variable are detected (e.g. fluoroquinolone association with %Ec-ESBL in Orihuela hospital population).

Step 7. Interpretation

The minimum thresholds identified for each significantly associated antibiotic group were translated into suggested maximum numbers of patient treatment courses per month not expected to adversely affect resistance at population levels. We multiplied the threshold, expressed in DDDs per 1000 OBDs (or IDs), by the size of the monthly patient population (in thousands of OBDs or IDs), and then divided by an average patient treatment course of 7 DDDs (except for aminoglycosides which were considered as 3 DDDs). These maximums were further compared to contemporary levels of antibiotic use in the last year of study, to

provide indications of how current use of antibiotics should be modified to avoid resistance spread.

Projections for alternative antibiotic stewardship policy options

To illustrate the potential effects of restricting antibiotics associated with %Ec-ESBL+ to threshold levels in populations of Orihuela, we compared the expected evolution of %Ec-ESBL+ under a ‘business as usual’ scenario in which antibiotic use continued as in last year of study, to projected time-series with antibiotics restricted to threshold levels. We used a breakpoint analysis to identify the last stationary segment in %Ec-ESBL+ time-series from the study period. We recursively estimated MARS models using means from these stationary segments as starting points to derive steady states for %Ec-ESBL+ in community and hospital populations. Based on steady state values and MARS models for the study period (baseline) we simulated 1000 samples of 24-month projections, incorporating random error term with variance as derived in the baseline MARS model. For each sample projection we entered mean antibiotic levels in the last year of the study period (‘business as usual’) and alternative levels set at identified thresholds. We calculated the mean difference between business as usual and each policy option for every month along with 95% confidence intervals. Finally, we illustrated alternative projections and differences using medians of distributions from the 1,000 sample projections.

Data availability

The data that support the findings of this study are available from the corresponding author upon reasonable request.

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Supplementary information

Is available in the online version of the article

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Author contributions

J-M.L-L., T.L., C.N., A.B., and I.M.G., proposed the original idea and designed the study. X.B., D.H., M.A., G.C-B., M.S., D.F., G.K., J.R-B., P.R., and N.G., collated centre-specific data, situational analysis, and hypotheses. J-M.L-L., T.L., C.N., A.B., contributed to statistical analysis, with C.N. and A.B, the principal analysts. All authors discussed the results and commented on the manuscript.

Competing interests

IMG is in receipt of payments for consultancies and lectures from numerous Pharmaceutical firms developing new antimicrobials. Otherwise, the authors declare no competing interests.

Figure legends

Figure 1 | Carbapenem-resistant *A. baumannii* and antibiotic use

(a) Time series for observed and predicted incidence density of CRAb, with observed incidence density of CSAb. (b) Time series for use of potential explanatory antibiotic groups (5-month moving averages). (c) Contribution charts illustrating the relationship between explanatory variables and CRAb incidence density (sample size, n=143 months of observation).

^a Change relative to median monthly CRAb incidence density for study period.

CRAb, carbapenem-resistant *A. baumannii*. CSAb, carbapenem-susceptible *A. baumannii*.

DDDs, defined daily doses. IQR, Interquartile range. MARS, Multivariate Adaptive

Regression Splines. NL-TSA, non-linear time series analysis. OBDs, occupied bed days.

Figure 2 | Extended-spectrum β -lactamase (ESBL)-producing *Escherichia coli* and antibiotic use in hospital and community.

(a) Time series for observed and predicted %Ec-ESBL+ in hospital population. (b) Time series of potential explanatory antibiotic groups in hospital population (5-month moving averages). (c) Time series for observed and predicted %Ec-ESBL+ in community population. (d) Time series of potential explanatory antibiotic groups in community population (5-month moving averages). (e) Contribution charts illustrating the relationship between explanatory variables and hospital or community %Ec-ESBL+. (sample size, n=304 months of observation).

^a compared to median monthly %Ec-ESBL+ for study period.

* confidence interval around lower threshold in association between fluoroquinolones and %Ec-ESBL+ in hospital may be wider due to risk of slight under-coverage of confidence interval estimation arising from a problem of multiple closely occurring thresholds.

%Ec-ESBL+, percentage of *E. coli* isolates producing extended-spectrum beta-lactamases.

DDDs, defined daily doses. IQR, Interquartile range. MARS, Multivariate Adaptive

Regression Splines. NL-TSA, non-linear time series analysis. OBDs, occupied bed days.

Figure 3 | Cefepime-resistant *Escherichia coli* and antibiotic use

(a) Time series for observed and predicted incidence density of %Ec-FepR. (b) Time series of potential explanatory antibiotic groups (5-month moving averages). (c) Contribution charts illustrating the relationship between explanatory variables and %Ec-FepR (sample size, n=105 months of observation).

^a compared to median monthly %Ec-FepR for study period.

DDDs, Defined Daily Doses. IQR, interquartile range. %Ec-FepR, percentage of *E. coli*

isolates resistant to cefepime. OBDs, Occupied Bed Days.

Figure 4: Gentamicin-resistant *Pseudomonas aeruginosa* and antibiotic use

(a) Time series for observed and model predicted incidence density of GRPa. (b) Time series of potential explanatory antibiotic groups (5-month moving averages) (c) Contribution charts illustrating the relationship between explanatory variables and GRPa incidence density

^a compared to median monthly GRPa incidence density for study period (sample size, n=192 months of observation).

DDDs, Defined Daily Doses. GRPa, gentamicin-resistant *P. aeruginosa*; GSPa, gentamicin-

susceptible *P. aeruginosa* isolates. IQR, Interquartile range. MARS, multivariate adaptive

regression splines OBDs, Occupied Bed Days.

Figure 5: Methicillin-resistant *Staphylococcus aureus*, hand hygiene, and antibiotic use
(a) Time series for observed and predicted incidence density of MRSA. **(b)** Time series of potential explanatory antibiotic groups (5-month moving averages). **(c)** Time series for alcohol-based hand rub (ABHR) use. **(d)** Contribution charts illustrating the relationship between explanatory variables and MRSA incidence density (sample size, n=105 months of observation).

^a compared to median monthly MRSA incidence density for study period.

ABHR, alcohol-based hand rub. DDDs, Defined Daily Doses. ECDC, European Centre for Disease Prevention and Control. MRSA, Methicillin-resistant *Staphylococcus aureus*. OBDs, Occupied Bed Days.

Tables

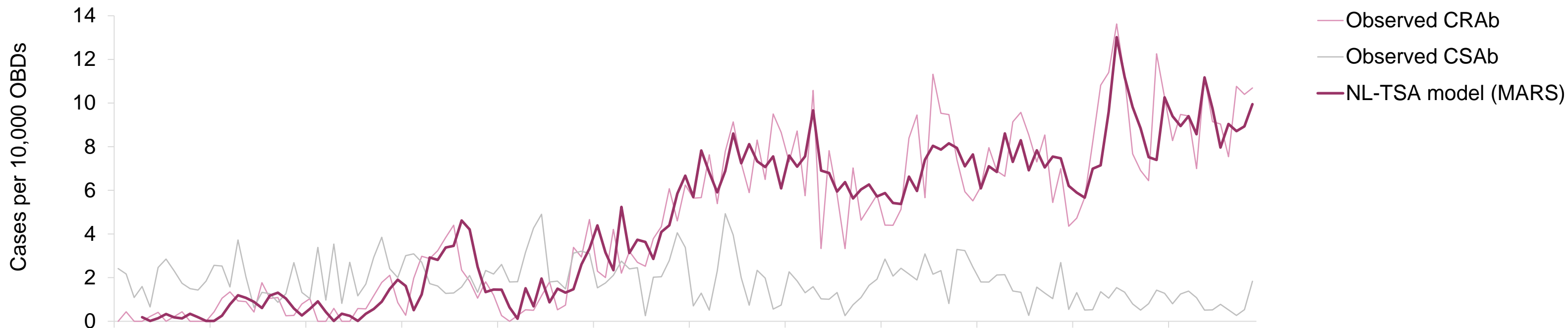
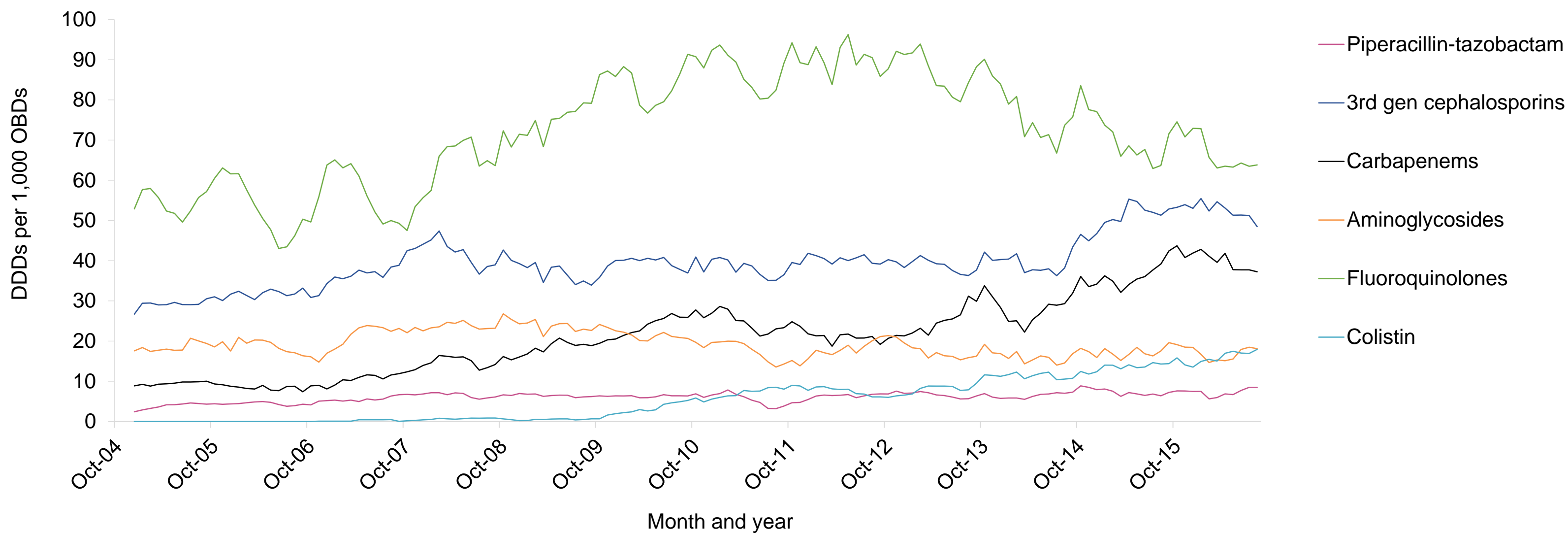
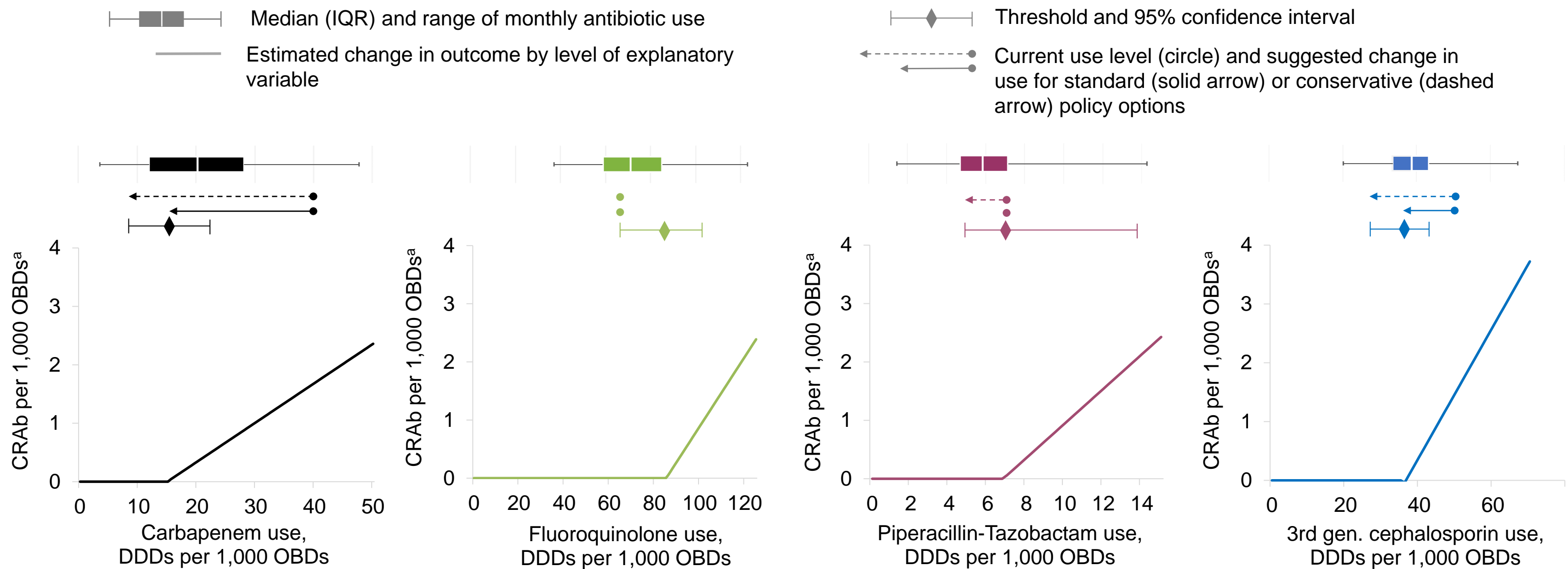
Table 1: Translation of thresholds identified in non-linear models into population-specific antibiotic stewardship policy recommendations

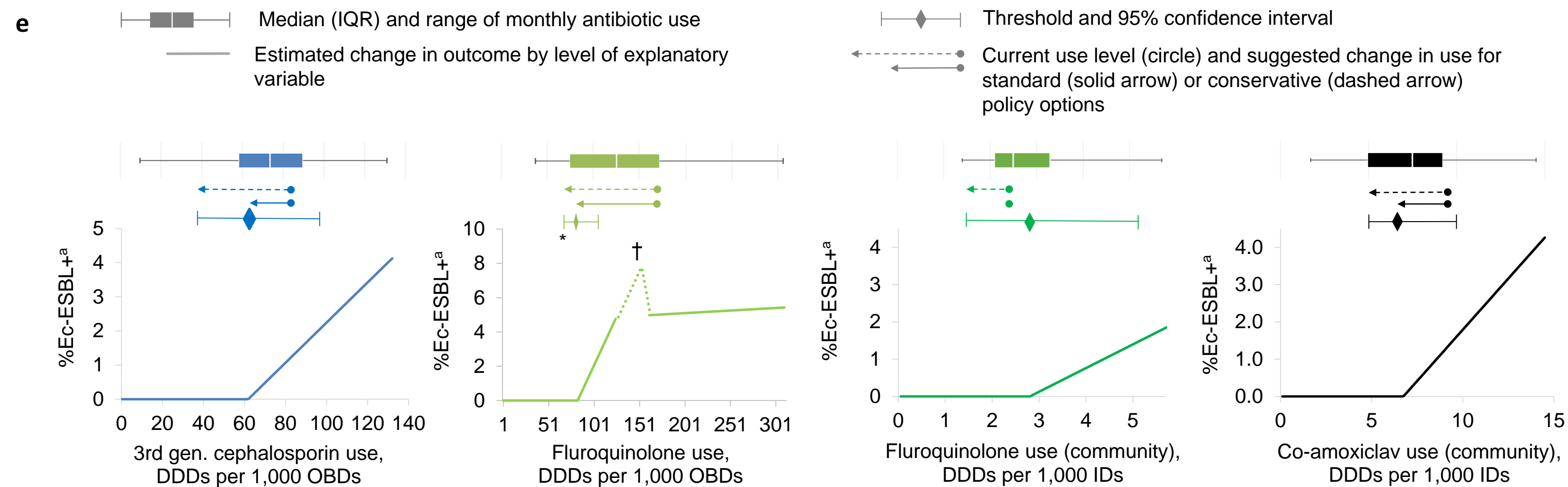
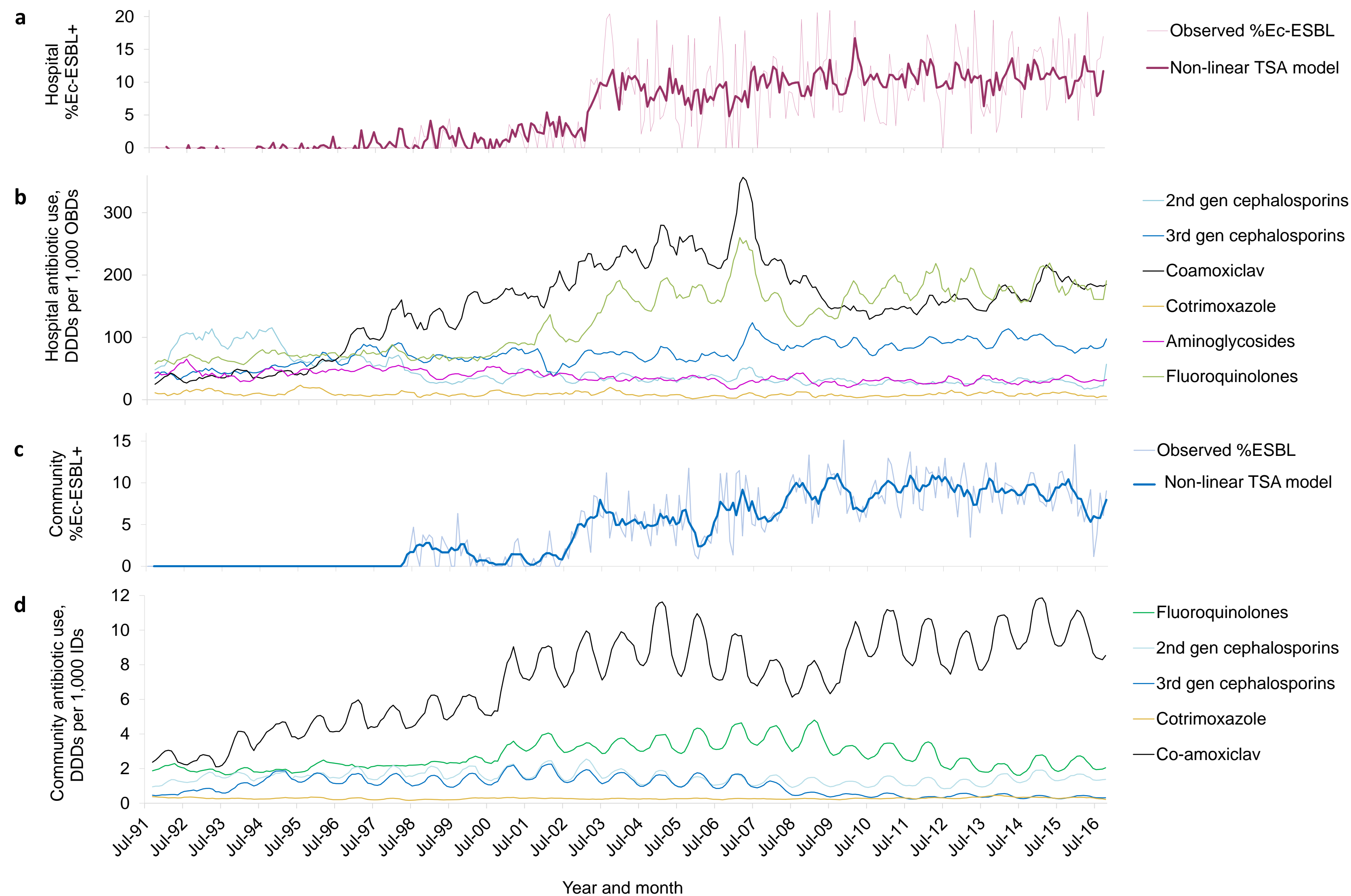
Antibiotic	Patient treatments per month ^a			
	Maximum suggested by threshold (95% CI)	Average use in last 12 months of study	Suggested reduction in use (%)	
			Standard (using point estimate for threshold)	Conservative (using lower limit of 95% CI for threshold)
1. Carbapenem-resistant <i>Acinetobacter baumannii</i> (CRAB)[‡] Debrecen, Hungary				
Carbapenems	86 (45 to 134)	226	140 (62%)	181 (80%)
3 rd generation cephalosporins	203 (169-229)	299	96 (32%)	130 (57%)
Fluoroquinolones	478 (367-576)	375	Maintain below threshold	9 (2%)
Piperacillin-tazobactam	39 (28-78)	41	2 (5%)	13 (32%)
2. Extended-spectrum β-lactamase producing <i>Escherichia coli</i> (%Ec-ESBL+) Orihuela, Spain				
<i>a) Hospital population</i>				
Fluoroquinolones	78 (67 to 96) ^b	165	68 (41%)	87 (53%) ^b
Third-generation cephalosporins	62 (35 to 91)	78	16 (21%)	43 (55%)
<i>b) Community population</i>				
Fluoroquinolones	80 (40 to 148)	66	Maintain below threshold	26 (39%)
Co-amoxiclav	191 (142 to 284)	277	86 (31%)	135 (49%)
3. Cefepime-resistant <i>Escherichia coli</i> (%EcFepR) Seville, Spain				
Fluoroquinolones	392 (225 to 426)	351	Maintain below threshold	126 (36%)
3 rd /4 th generation cephalosporins	130 (83 to 158)	211	87 (41%)	128 (61%)
4. Gentamicin-resistant <i>Pseudomonas aeruginosa</i> (GRPa) , France				
Gentamicin and tobramycin	75 (36-99) ^b	68 ^c	Maintain below threshold	32 (47%)
Fluoroquinolones	324 (316 to 330)	223	Maintain below threshold	Maintain below threshold
5. Methicillin-resistant <i>Staphylococcus aureus</i> (MRSA) Antrim, Northern Ireland				
Fluoroquinolones	24 (20 to 29)	39	15 (39%)	19 (49%)
3 rd generation cephalosporins	7 (6 to 8)	6	Maintain below threshold	Maintain below threshold
Co-amoxiclav	320 (189 to 422)	320	Maintain below threshold	131 (41%)

^a Derived by multiplying the threshold in table 1, expressed in DDDs per 1000 OBDs, by the size of the population (in 1000 OBDs or IDs), and then dividing by an average patient treatment (considered as 7 DDDs unless otherwise specified)

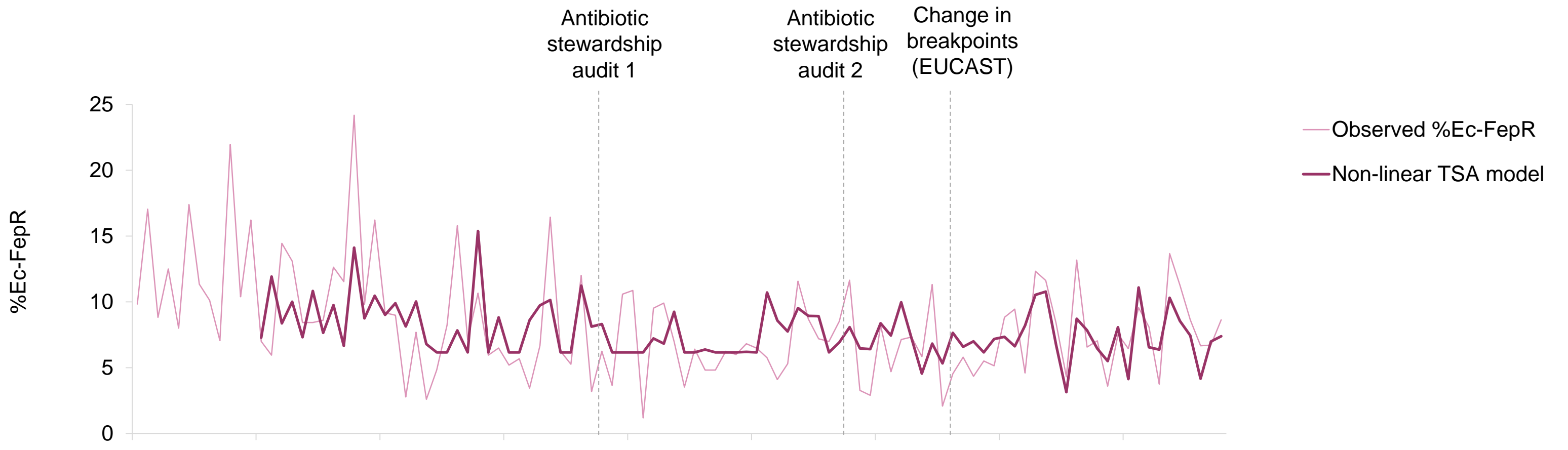
^b Confidence intervals may be wider, and the recommended restriction greater in the conservative approach, due to risk of slight undercoverage of estimated confidence intervals due to multiple closely occurring thresholds in association between fluoroquinolone and %Ec-ESBL+ in hospital.

^c Average treatment course considered as 3 DDDs.

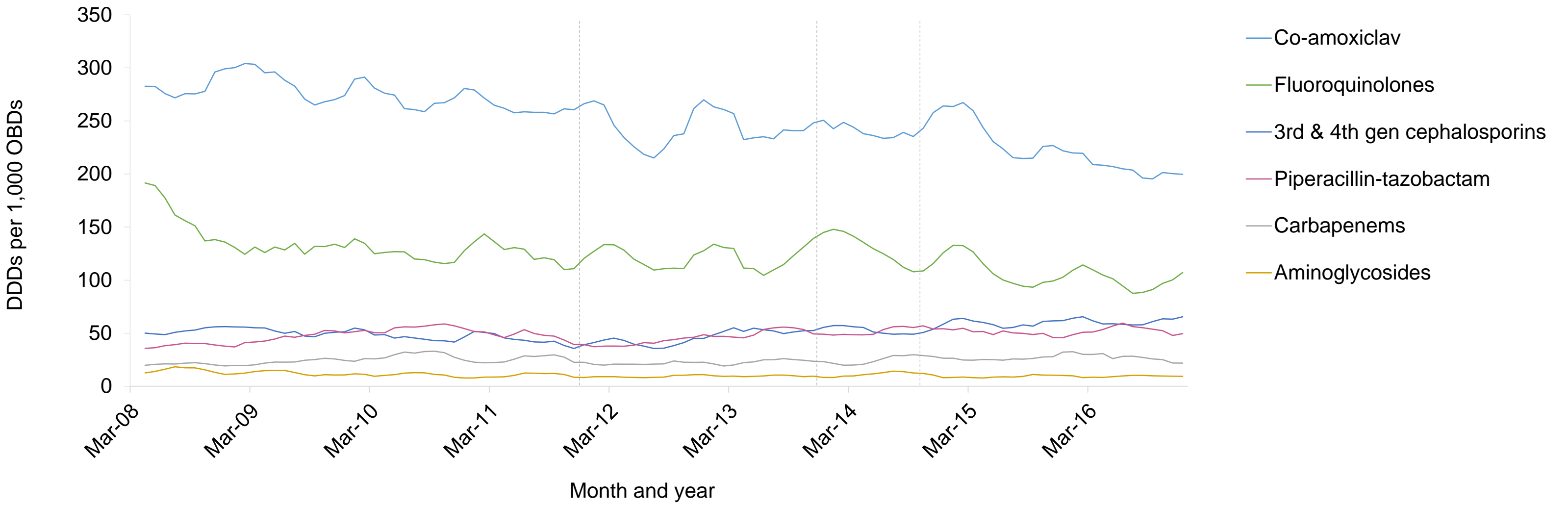
a**b****c**



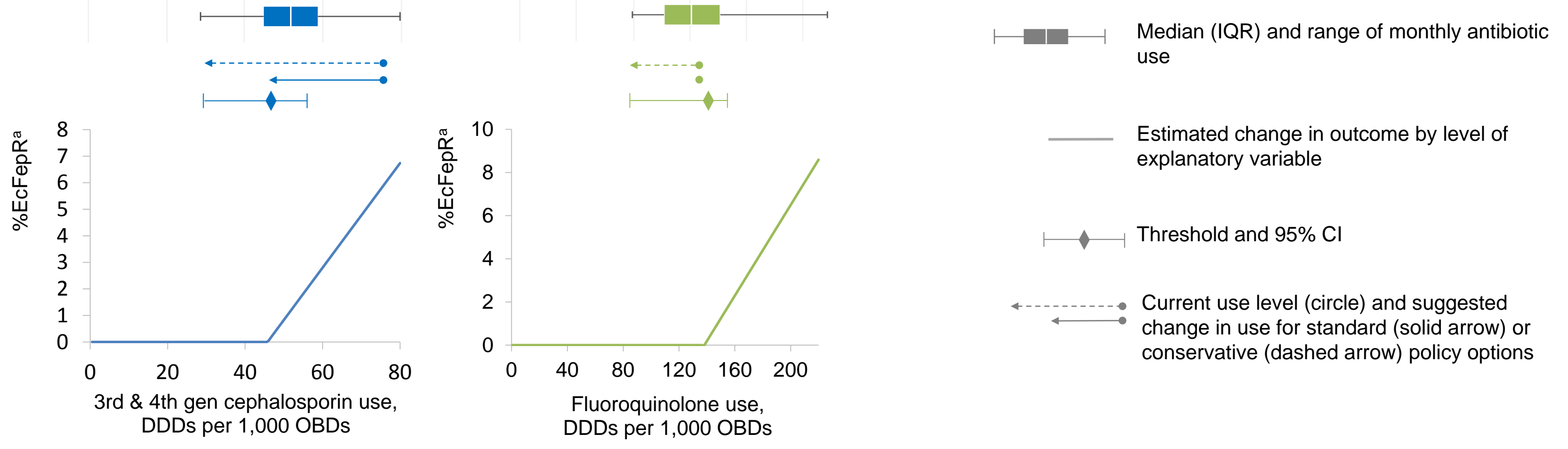
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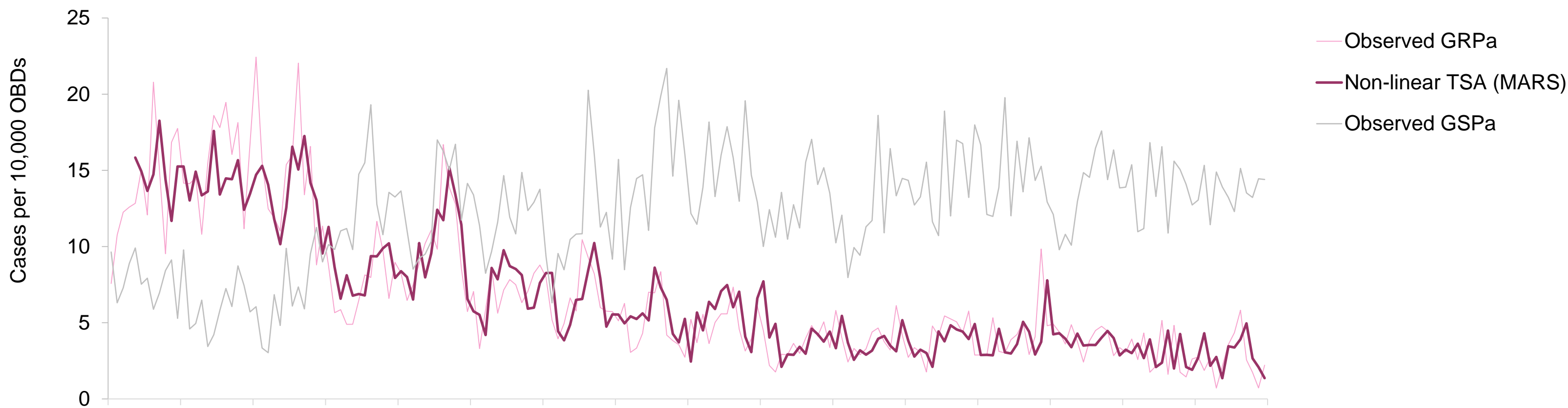
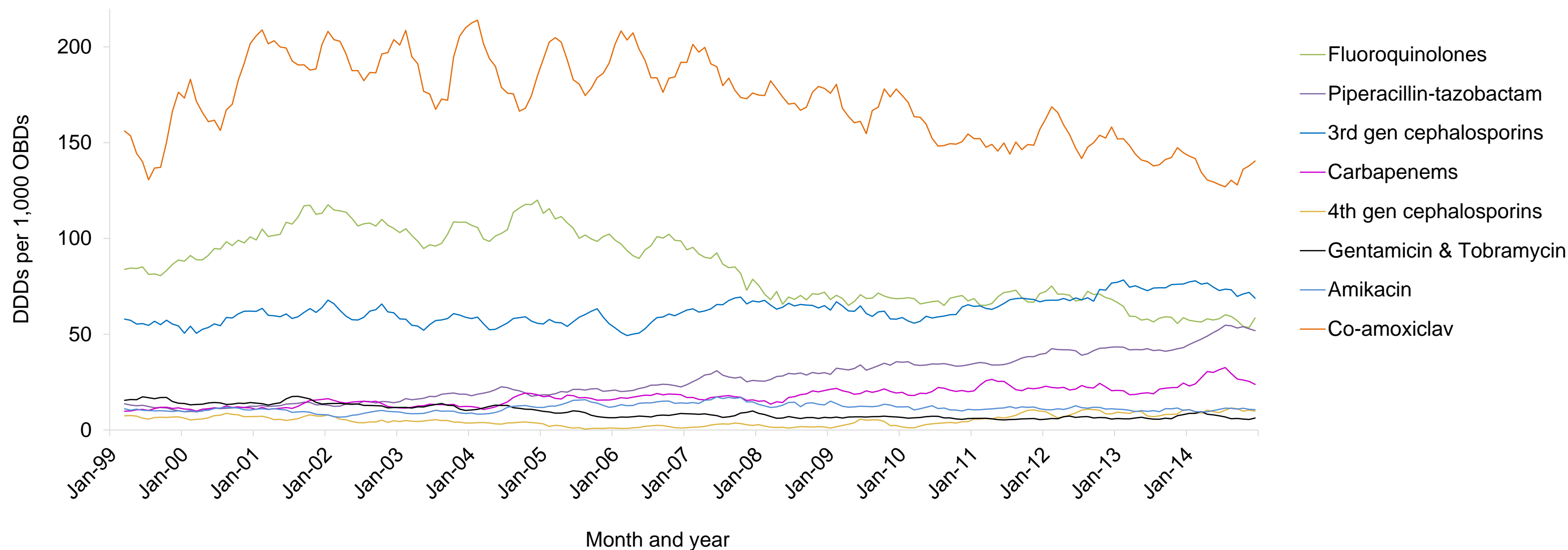


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